Aim: To solve a differential equation using modified Euler's Method.

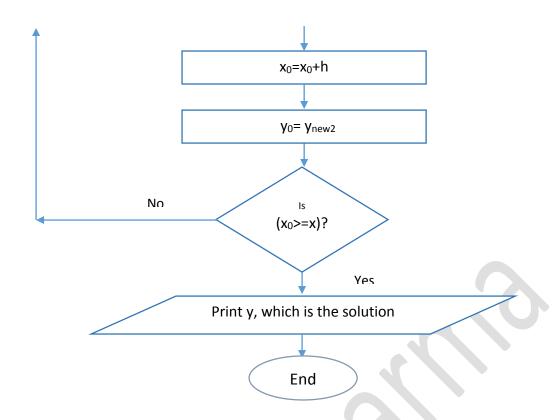
Algorithm:

- 1. Enter the initial values of x and $y(x_0,y_0)$.
- 2. Enter the value of x for which y is to be determined.
- 3. Enter the width of the interval, 'h'.
- 4. Do:

```
slope_1 = dy/dx_{(x0,y0)}
y_{new} = y_0 + (h*slope_1)
slope_2 = dy/dx_{(x0,ynew)}
slope_{avg} = slope_1 + slope_2
y_{new2} = y_0 + h*slope_{avg}.
x_0 = x_0 + h
y_0 = y_{new2}
Until (x_0 > = x)
```

5. Print y, which is the solution.

Flow Chart: Start Enter x₀ and y₀ Enter the value of x for which y is to be determined Enter the width of the interval, 'h' $slope_1 = dy/dx_{(x0,y0)}$ $y_{new}=y_0+(h*slope_1)$ $slope_2=dy/dx_{(x0,ynew)}$ slope_{avg}=slope₁+slope₂ $y_{new2}=y_0+h*slope_{avg}$.



Program:

```
//Modified Euler's Method for differential equations
#include<iostream>
#include<iomanip>
#include<cmath>
using namespace std;
double df(double x, double y)
    double a=x+y;
                             //function for defining dy/dx
    return a;
int main()
    double x0, y0, x, y_i, dy1, dy2, dy_avg, y_n, h;
                                              //for initial values,
width, etc.
    cout<<"\nEnter the initial values of x and y respectively:\n";</pre>
    cin>>x0>>y0;
                                    //Initial values
    cout<<"\nEnter the value of x for which you would like to find y:\n";</pre>
    cin>>x;
    cout<<"\nEnter the interval width,h:\n";</pre>
    cin>>h;
                                   //input width
cout < "x" < setw (16) < "y" < setw (16) < "hy'" < setw (16) < "y new" < setw (16) < "hy
new'"<<setw(16)<<"hy'avg"<<setw(16)<<"y n+1"<<endl;
    cout<<"-----
----\n";
    while (fabs(x-x0)>0.0000001
                                   //I couldn't just write "while(x0<x)"
as they both are floating point nos. It is dangerous to compare two
floating point nos. as they are not the same in binary as they are in
decimal. For instance, a computer cannot exactly represent 0.1 or 0.7 in
binary just like decimal can't represent 1/3 exactly without recurring
digits.
```

```
{
         dy1=h*df(x0,y0);
                                    //calculate slope or dy/dx at x0,y0
         y_i=y0+dy1;
                                  //calculate new y, which is y0+h*dy/dx
         dy2=h*df(x0,y_i);
                                    //calculate slope or dy/dx at x0, new y
         dy avg = (dy1 + dy2)/2.0;
                                         //calculate the average of the slopes
at y0 and new y
        y n=y0+dy avg;
                                     //calculate new y, which is
y0+h*average(dy/dx)
\verb|cout|<< x0<< \verb|setw|(16)|<< y0<< \verb|setw|(16)|<< y_i<< \verb|setw|(16)|<< y_i<< \verb|setw|(16)|<< y_i<< setw|(16)|< |
6) <<dy_avg<<setw(16) <<y_n<<endl;</pre>
        x0=x0+h;
                               //calculate new x.
         y0=y n;
                                   //pass this new y as y0 in the next
iteration.
    cout << x0 << setw (16) << y0 << endl;
    cout<<"The approximate value of y at x=0 is "<<y0<<endl;</pre>
                                                                         //print the
solution.
   return 0;
}
```

Outputs:

For dy/dx=x+y

```
Enter the initial values of x and y respectively:
Enter the value of x for which you would like to find y:
Enter the interval width,h:
0.1
                             hy'
                                                         hy_new'
                                           y_new
                                                                          hy'avg
                                                                                           y_n+1
                             0.1
                                             1.1
                                                            0.11
                                                                           0.105
0.1
             1.105
                            0.1205
                                            1.2255
                                                           0.13255
                                                                          0.126525
                                                                                           1.23152
                                           1.37468
                                                          0.157468
           1,23152
                          0.143152
                                                                           0.15031
                                                                                           1.38184
0.2
                          0.168184
                                           1.55002
                                                          0.185002
                                                                          0.176593
                                                                                           1.55843
0.3
           1.38184
0.4
           1.55843
                          0.195843
                                           1.75427
                                                          0.215427
                                                                          0.205635
                                                                                           1.76406
0.5
           1.76406
                           0.226406
                                           1.99047
                                                          0.249047
                                                                          0.237727
                                                                                           2.00179
           2.00179
                          0.260179
                                           2.26197
                                                          0.286197
                                                                          0.273188
                                                                                           2.27498
0.6
0.7
           2.27498
                          0.297498
                                           2.57247
                                                          0.327247
                                                                          0.312373
                                                                                           2.58735
                                                                                           2.94302
0.8
           2.58735
                          0.338735
                                           2.92608
                                                          0.372608
                                                                          0.355672
                          0.384302
           2.94302
                                           3.32732
                                                          0.422732
                                                                          0.403517
                                                                                           3.34654
0.9
         3.34654
The approximate value of y at_x=0 is 3.34654
```

For dy/dx=-2x-y

```
Enter the initial values of x and y respectively: 0 -1
Enter the value of x for which you would like to find y:
Enter the interval width,h:
.1
x
---
                              hy'
                                                           hy_new'
                                                                             hy'avg
                                             y_new
                                                                                              y_n+1
               -1
                              0.1
                                              -0.9
                                                              0.09
                                                                             0.095
                                                                                             -0.905
0.1
                                                                                            -0.838025
                             0.0705
                                             -0.8345
                                                             0.06345
                                                                             0.066975
             -0.905
                                           -0.794223
                                                           0.0394223
                                                                            0.0416124
                                                                                            -0.796413
          -0.838025
                          0.0438025
0.3
          -0.796413
                          0.0196413
                                           -0.776771
                                                           0.0176771
                                                                            0.0186592
                                                                                            -0.777753
          -0.777753
The approximate value of y at_x=0 is -0.777753
```