

# Interactive DEMO – Perform DFT based embedding in the cloud

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My name is [Manas Sharma](#), and I'm a Ph.D. student in the [Computational Materials Science group](#) of [Prof. Dr. Marek Sierka](#).

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## References

1. T. Wesolowski, A. Warshel, *J. Phys. Chem.* 97, 8050 (1993).
2. C. Müller, M. Sharma, M. Sierka, *J. Comput. Chem.* 41, 2573 (2020)
3. TURBOMOLE, a development of the University of Karlsruhe and Forschungszentrum Karlsruhe GmbH, 1989-2007, TURBOMOLE GmbH, since 2007; available from <http://www.turbomole.com>. (development version)
4. F. Furche, R. Ahlrichs, C. Hattig, W. Klopper, M. Sierka, F. Weigend, *WIREs Comput. Mol. Sci.* 4, 91 (2014).
5. R. Łazarski, A.M. Burow, M. Sierka, *J. Chem. Theory Comput.* 11, 3029 (2015).
6. D. Chulhai, J. Goodpaster, *J. Chem. Theory Comput.* 14, 1928-1942 (2018).
7. A. Krishtal, D. Ceresoli, M. Pavanello, *J. Chem. Phys.* 142, 154116 (2015).

## Poster

# Density Functional Theory Based Embedding Scheme for Molecular and Periodic Systems

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SCAN ME



ICQNN 2022  
05-09 Sept. 2022  
Jena, Germany

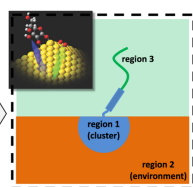
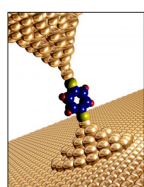
## INTRODUCTION

An implementation of density functional embedding theory (DFET), within the frozen density embedding (FDE) formalism<sup>[1]</sup>, using Gaussian basis functions is presented.

The implementation is coupled with real-time time-dependent DFT (RT-TDDFT)<sup>[2]</sup> and wavefunction theory (WFT) methods to perform RT-TDDFT-in-DFT and WFT-in-DFT, respectively.

**Highlights:** Molecule-in-molecule, molecule-in-periodic and periodic-in-periodic embedding within the TURBOMOLE program package<sup>[3-5]</sup>.

## DENSITY FUNCTIONAL EMBEDDING THEORY (DFET)



The central idea of DFET with a molecule attached to the surface of a nanostructure.

Region 1 (cluster) is the region of interest embedded in region 2 (environment).

$$E[\rho^{\text{tot}}] = E[\rho^{\text{clu}}] + E[\rho^{\text{env}}] + E^{\text{int}}[\rho^{\text{clu}}, \rho^{\text{env}}]$$

Density partition:

$$\rho^{\text{tot}} = \rho^{\text{clu}} + \rho^{\text{env}}$$

Total Energy

$$E[\rho^{\text{tot}}] = E[\rho^{\text{clu}}] + E[\rho^{\text{env}}] + E^{\text{int}}[\rho^{\text{clu}}, \rho^{\text{env}}]$$

The key quantity in DFET is a DFT based embedding potential  $v_{\text{emb}}$  which can be defined in an approximate or exact manner as

**Embedding potential (Approximate)**

$$v_{\text{emb}}[\rho^{\text{act}}, \rho^{\text{env}}, v_{\text{nuc}}^{\text{env}}](\mathbf{r}) = v_{\text{nuc}}^{\text{env}}(\mathbf{r}) + \int \frac{\rho^{\text{env}}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{\text{xc}}^{\text{nadd}}[\rho^{\text{act}}, \rho^{\text{env}}]}{\delta \rho^{\text{act}}(\mathbf{r})} + v_T[\rho^{\text{act}}, \rho^{\text{env}}](\mathbf{r})$$

with non-additive kinetic potential

$$v_T[\rho^{\text{act}}, \rho^{\text{env}}](\mathbf{r}) = \frac{\delta T_s^{\text{nadd}}[\rho^{\text{act}}, \rho^{\text{env}}]}{\delta \rho^{\text{act}}(\mathbf{r})} = \frac{\delta T_s[\rho^{\text{tot}}]}{\delta \rho^{\text{tot}}(\mathbf{r})} - \frac{\delta T_s[\rho^{\text{act}}]}{\delta \rho^{\text{act}}(\mathbf{r})}$$

where  $T_s$  is evaluated using approximate kinetic energy density functional (KEDF)

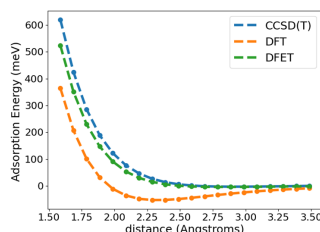
**Embedding potential (Exact)**

In matrix form

$$\mathbf{V}_{\text{emb}} = \mathbf{V}_{\text{nuc}}^{\text{env}} + \mathbf{J}_{\text{elec}}^{\text{env}} + \mathbf{X}_{\text{nadd}} + \mathbf{P}_B$$

with Projection operator:  $\mathbf{P}_B = \mu \mathbf{S}^{\text{AB}} \mathbf{D}^{\text{B}} \mathbf{S}^{\text{BA}}$  with  $\mu = 10^6$

## MOLECULE-in-PERIODIC EMBEDDING



CCSD(T)-DFET much closer to regular CCSD(T) at just 10% of COMPUTATIONAL COST!!!

H<sub>2</sub> (molecule)

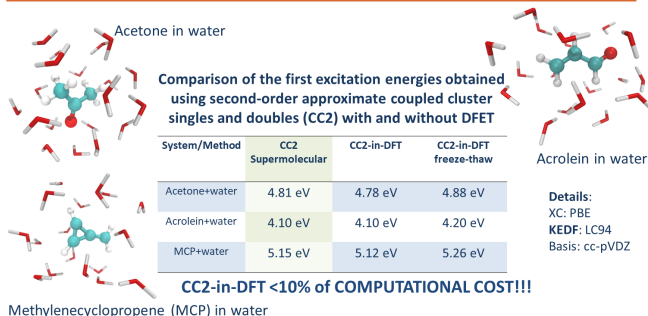
Colored atoms are treated as cluster



H<sub>10</sub> (1D periodic chain)



## MOLECULE-in-MOLECULE (WFT-in-DFT) EMBEDDING



Methylene cyclopropane (MCP) in water

## PERIODIC-in-PERIODIC EMBEDDING

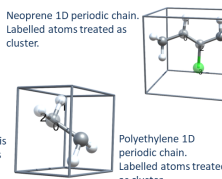
Total energies (Hartrees) obtained using periodic KS-DFT and DFET

System/Method	DFT	DFET
Polyethylene (gamma)	-78.3875751502	-78.3875735082
Polyethylene (32 k-points)	-78.4571146741	-78.4571160584
Neoprene (gamma)	-614.9728903786	-614.9728912891

Details:

- 1D Periodicity
- Basis: def2-SVP
- PBE-in-PBE DFET
- with Projection operator and supermolecular basis
- 5 freeze-thaw cycles

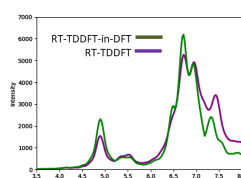
Neoprene 1D periodic chain. Labelled atoms treated as cluster.



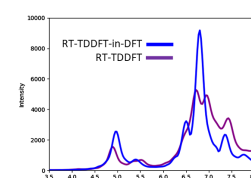
Polyethylene 1D periodic chain. Labelled atoms treated as cluster.

The embedding procedure is similar to the implementation of Chulhai *et al.* using PySCF<sup>[6]</sup>. However, in contrast to their implementation, the KS matrices here are calculated in real space. Furthermore, the Coulomb contributions are calculated using highly efficient density fitting and the continuous fast multipole methods<sup>[5]</sup>.

## RT-TDDFT-in-DFT



Benzene-Fulvene Dimer at 4 Angstrom separation



- using Projection Operator (5 freeze-thaw cycles), supermolecular basis and updating embedding potential

The environment density was kept frozen to the ground state density while the cluster was evolved in time.

- using nadd KEDF (5 freeze-thaw cycles), supermolecular basis and updating embedding potential

## CONCLUSION & OUTLOOK

- DFET (KEDF), coupled with WFT methods (WFT-in-DFT), offers reasonable accuracy for adsorption energy and excitation energies of weakly interacting systems with a significant reduction in computational cost.
- Supermolecular DFET (Projection) coupled with RT-TDDFT offers great accuracy, even for strongly interacting systems, and can play a crucial role in studying excitation energy transfer<sup>[7]</sup>.
- Periodic-in-periodic embedding paves the way for exact cluster-in-periodic RT-TDDFT/WFT calculations.

## References:

1. T. Wesolowski, A. Warshel, *J. Phys. Chem.* **97**, 8050 (1993).
2. C. Müller, M. Sharma, M. Sierka, *J. Comput. Chem.* **41**, 2573 (2020).
3. TURBOMOLE 7.5, a development of the University of Karlsruhe and Forschungszentrum Karlsruhe GmbH, 1989-2007, TURBOMOLE GmbH, since 2007, available from <http://www.turbomole.com> (development version)
4. F. Furche, R. Ahlrichs, C. Hättig, W. Klopper, M. Sierka, F. Weigend, *WIREs Comput. Mol. Sci.* **4**, 91 (2014).
5. R. Lazarski, A.M. Burow, M. Sierka, *J. Chem. Theory Comput.* **11**, 3029 (2015).
6. D. Chulhai, J. Goodpaster, *J. Chem. Theory Comput.* **14**, 1928–1942 (2018).
7. A. Krishtal, D. Ceresoli, M. Pavanello, *J. Chem. Phys.* **142**, 154116 (2015).



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# Video Presentation



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I'm a physicist specializing in computational material science with a PhD in Physics from Friedrich-Schiller University Jena, Germany. I write efficient codes for simulating light-matter interactions at atomic scales. I like to develop Physics, DFT, and Machine Learning related apps and software from time to time. Can code in most of the popular languages. I like to share my knowledge in Physics and applications using this Blog and a YouTube channel.

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