

While working on Fourier Series or some other Mathematical Problem, you might sometime have to work with Periodic Functions.

Periodic Functions are those that give the same value after a particular period.

So we will use this definition to define a periodic function in SCILAB.

Let's say that there is a function $f(x)$ which is periodic with a period of $2*T$ and is already defined in the interval $[-T, T]$.

Then the function should have the same value at: $f(x)$, $f(x+2*T)$, $f(x+4*T)$,

i.e. $f(x)=f(x+2*T)=f(x+4*T)=\dots\dots$ since $\text{period}=2*T$.

But I said that the function is defined only in the interval $[-T, T]$. So how is the computer supposed to calculate its value at $x > T$?

That's easy. Since the value of the function at $f(x+2*T)$ is simply $f(x)$, therefore we can generalize that whenever $x > T$: then,

$f(x)=f(x-2*T)$. Note: We have to keep taking x back by $2*T$ i.e $(x-2*T)$ until it lies within $[-T, T]$ where the function is well-defined.

Similarly what about the value of function at x less than $(-T)$ cause the function is not defined for values less than $(-T)$?

Again, this time we use: $f(x)=f(x+2*T)$. Note: We keep translating x forward by $2*T$ i.e $(x+2*T)$ until it lies within $[-T, T]$ where the function is well-defined.

Using the above two arguments we can create a function which will make any given function defined within $[-T, T]$ and with a period $2*T$ a periodic function.

Here is the code for that:

```
//Periodic Function
function a=periodicf(T,f,x)
    if (x>=-T)&(x<=T) then
        a=f(x);
    elseif x>T then
        x_new=x-2*T;
        a=periodicf(T,f,x_new);
    elseif x<(-T) then
        x_new=x+2*T;
        a=periodicf(T,f,x_new);
    end
endfunction
```

Demo:

```

deff('a=f(x)', 'a=x');
-->periodicf(2,f,0)
ans =
0.

-->periodicf(2,f,1)
ans =
1.

-->periodicf(2,f,2)
ans =
2.

-->periodicf(2,f,3)
ans =
- 1.

-->periodicf(2,f,4)
ans =
0.

```

In the above example I have created a function $f(x)=x$.

Then I called the function 'periodicf' with $T=2$ (meaning period is 4) and passed the function 'f' as the second argument and then the third argument is the value of x at which I want the value of 'f'.

The above code assumes the function to be defined within $[-T, T]$ therefore the function's starting point is $(-T)$. However, if you want to create a function that is defined in a different manner then you will have to define 'f' correspondingly.

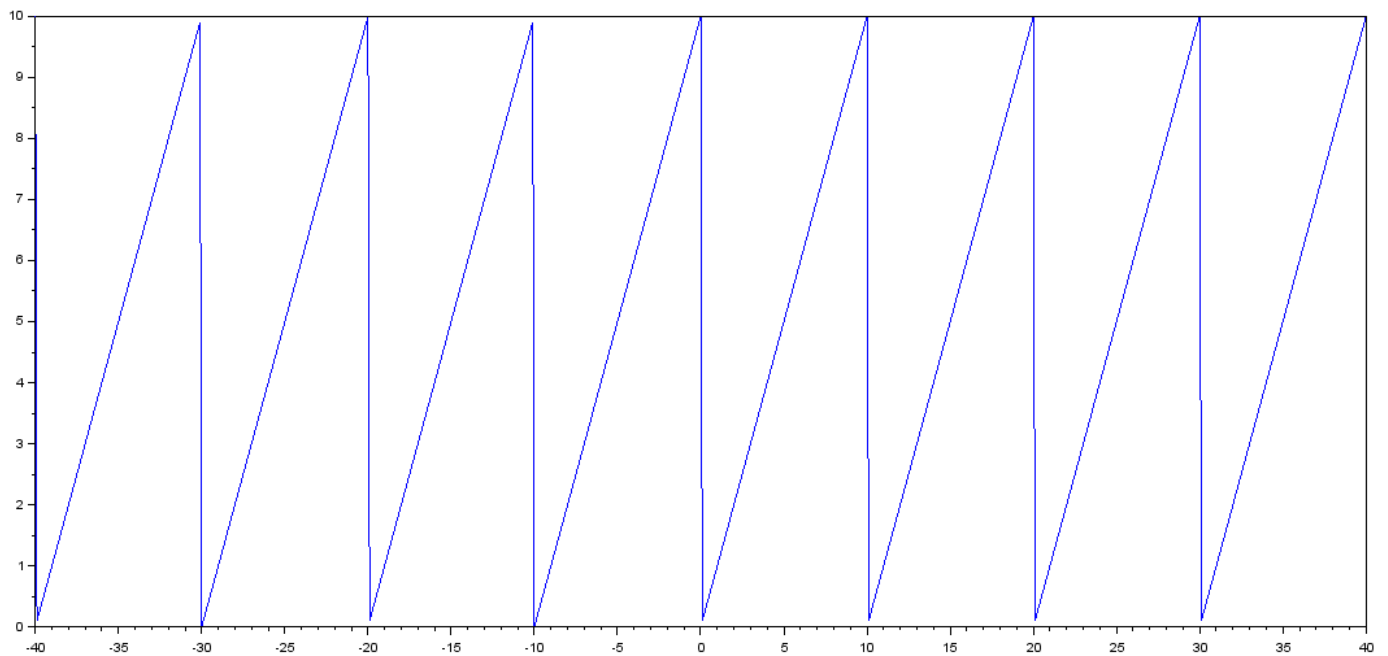
Following are some examples of different kinds of periodic functions along-with their plots:

Saw-tooth Wave(1):

Code:

```
//Saw-Tooth Wave(all Positive)
funcprot(0);
function a=sawtooth(T,x)
    deff('a=sawtooth_temp(x)','if x>0 then; a=x; else; a=x+T; end;');
    a=periodicf(T,sawtooth_temp,x);
endfunction
//Plotting a saw-tooth wave
x=[-40:0.1:40];
for i=1:801
    y(i)=sawtooth(5,x(i));
end
plot(x,y);
```

Output:

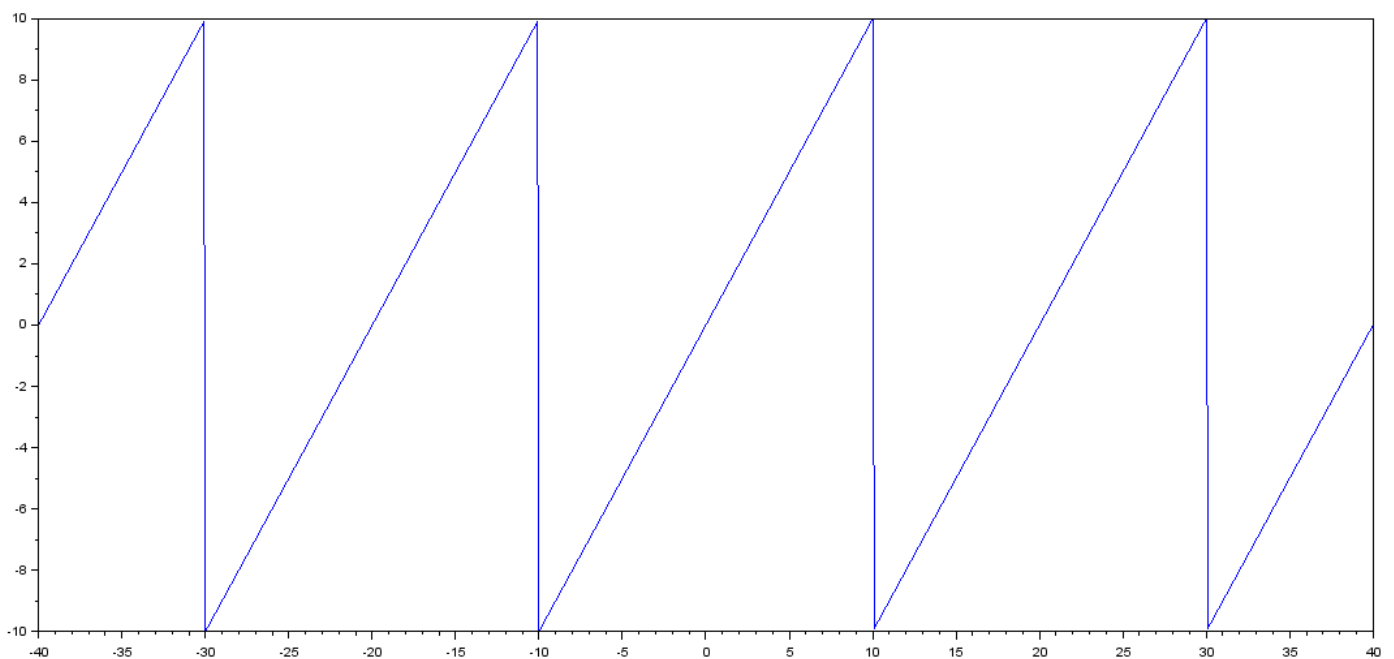


Saw-Tooth(2) Wave:

Code:

```
//Sawtooth wave(2)
funcprot(0);
function a=sawtooth2(T,x)
    deff('a=sawtooth_temp(x)','a=x');
    a=periodicf(T,sawtooth_temp,x);
endfunction
//Plotting a saw-tooth wave
x=[-40:0.1:40];
for i=1:801
    y(i)=sawtooth2(10,x(i));
end
plot(x,y);
```

Output:

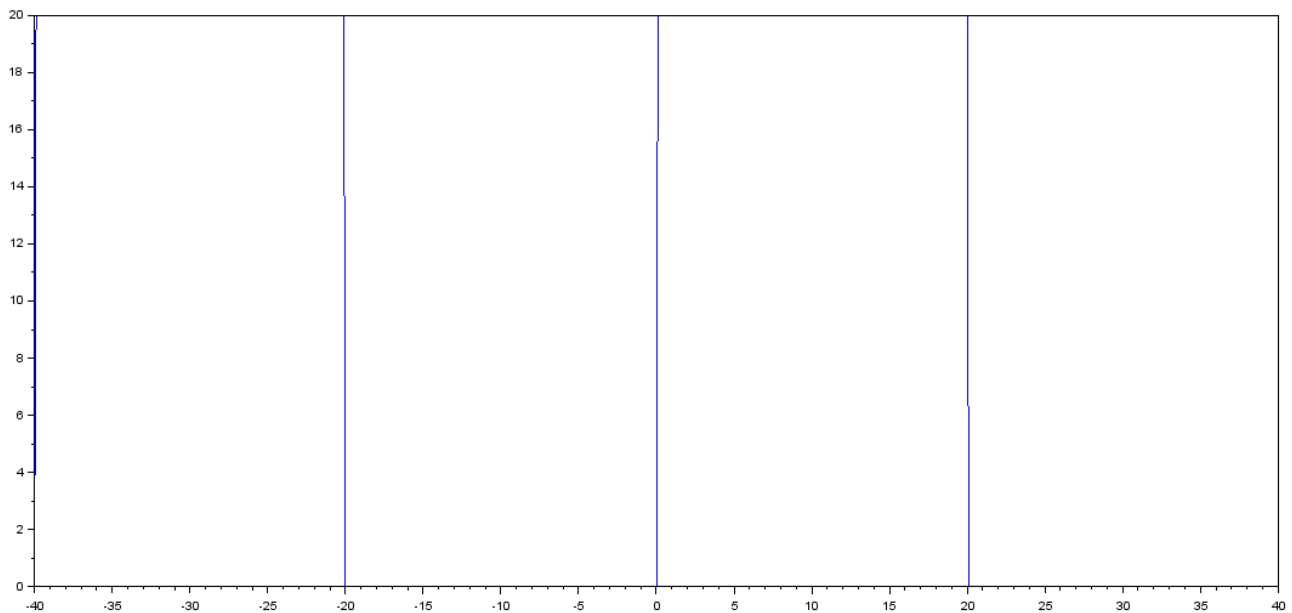


Square Wave(or Rectangle Wave) :

Code:

```
//Square-Wave or Rectangle Wave
funcprot(0);
function a=sqrwave(T,A,x)
    deff('a=sqwavetmp(x)','if x>0 then; a=A; else; a=0; end')
    a=periodicf(T,sqwavetmp,x);
endfunction
//Plotting a square wave
x=[-40:0.1:40];
for i=1:801
    y(i)=sqrwave(20,20,x(i));
end
plot(x,y);
```

Output:

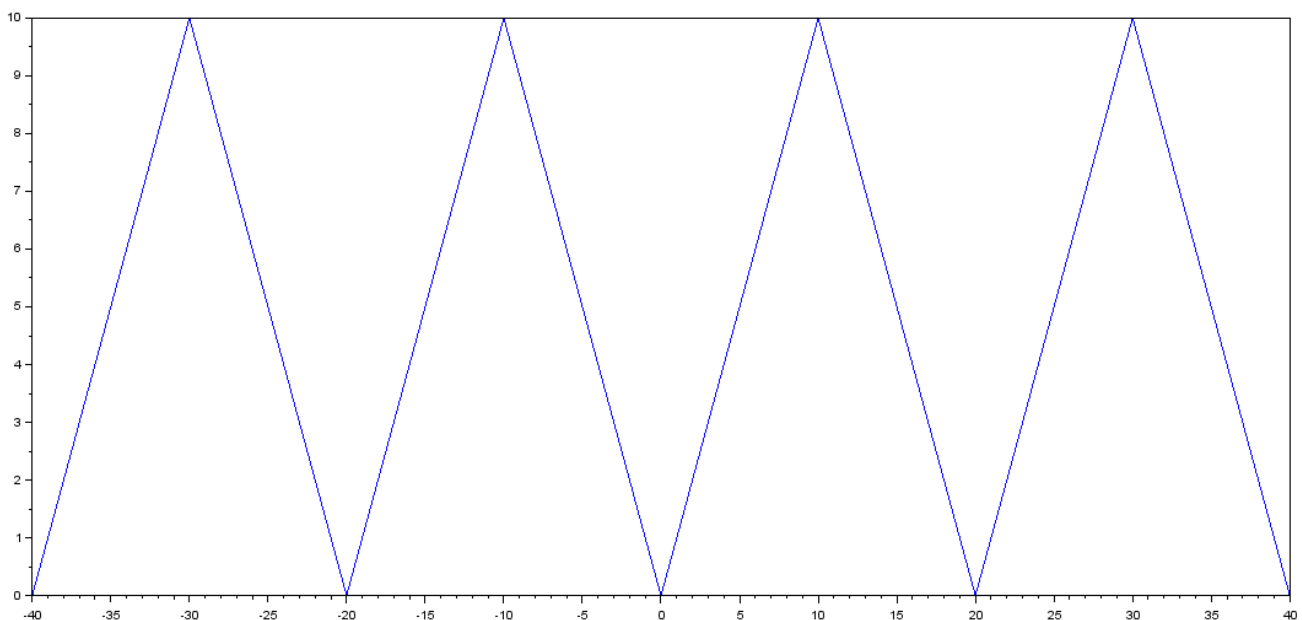


Triangular Wave:

Code:

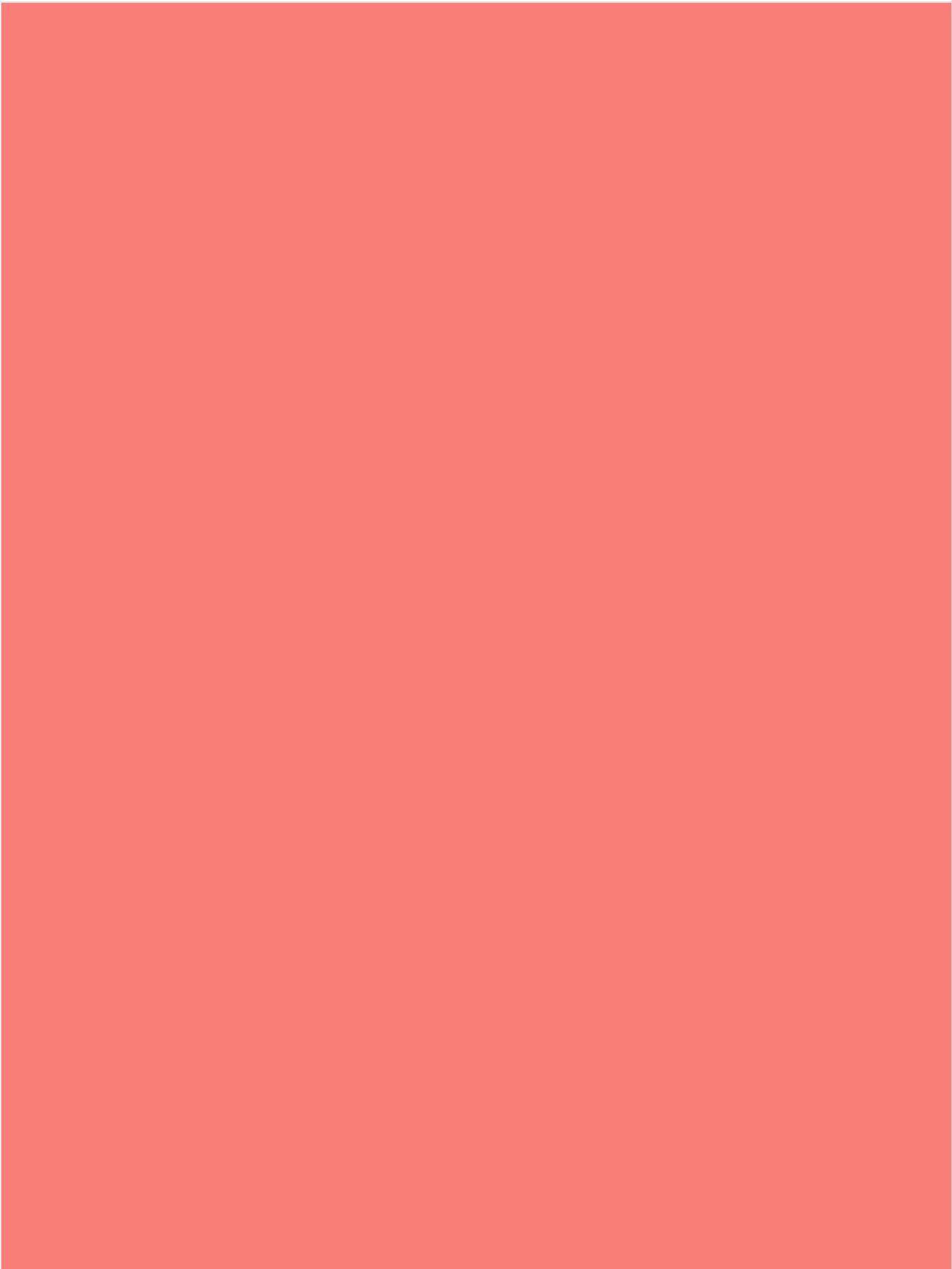
```
//Triangle Wave:
funcprot(0);
function a=trianglewave(T,x)
    deff('a=trnglewavetmp(x)','if x>0 then; a=x; else; a=-x; end')
    a=periodicf(T,trnglewavetmp,x);
endfunction
//Plotting a Triangle wave
x=[-40:0.1:40];
for i=1:801
    y(i)=trianglewave(10,x(i));
end
plot(x,y);
```

Output:



Manas Sharma

I'm a physicist specializing in computational material science with a PhD in Physics from Friedrich-Schiller University Jena, Germany. I write efficient codes for simulating light-matter interactions at atomic scales. I like to develop Physics, DFT, and Machine Learning related apps and software from time to time. Can code in most of the popular languages. I like to share my knowledge in Physics and applications using this Blog and a YouTube channel.



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